# **Power Electronics**

### INVERTERS

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## **Inverter Classification**

#### Classification of inverters based on wave shape

- Square wave
- Quasi square wave
- □ Sine wave

#### Classification of inverters based on Input

- Voltage source
- Current source



# Half bridge inverter



- Switches S1 and S2 used are gate commutated devices such as BJT, MOSFET, IGBT, GTO etc
- S1 and S2 are turned on alternately to produce an ac voltage across the load
- Each switch is ON for half time period (T/2) of the desired frequency

# Full bridge inverter



- □ S1 and S2 turned on in the first half cycle (T/2)
- □ S3 and S4 turned on in the second half cycle (T/2)

## Full bridge inverter – R load







- Mode 2: D3, D4 conducts, Output -ve
- Mode 3: S3 and S4 are ON, Output -ve
- Mode 4: D1, D2 conducts, Output +ve



## Full Bridge Inverter – Transistor Ratings



$$V_{CE(0)} \ge E_{DC}$$

$$I_{T(ave)} = \frac{E_{DC}}{2R}$$

$$I_{T(peak)} = \frac{E_{DC}}{R}$$

## Harmonics



Fourier series for symmetrical square wave, e =

$$=\sum_{n=1,3,5,\dots}^{\infty}\frac{4E_{DC}}{n\pi}\sin\left(n\ \omega t\right)$$

## Harmonics

Fourier Series, 
$$e = \sum_{n=1,3,5,..}^{\infty} \frac{4E_{DC}}{n\pi} \sin(n \omega t)$$

Fundamental output voltage,  $E_1 = \frac{2\sqrt{2}}{\pi} E_{DC}$ (rms) *ie.*  $E_1 = 0.9 E_{DC}$ 



n<sup>th</sup> order output voltage, 
$$E_n = \frac{E_1}{n}$$

RMS value, 
$$E_{(rms)} = \sqrt{E_1^2 + E_3^2 + E_5^2 + ...}$$
  
Harmonic voltage,  $E_h = \left(\sum_{n=3,5,..}^{\infty} E_n^2\right)^{\frac{1}{2}} = \left(E^2 - E_1^2\right)^{\frac{1}{2}} = 0.4352 E_{DC}$ 

## Harmonic Parameters

Harmonic factor for n<sup>th</sup> harmonic measures the individual harmonic contribution

Harmonic Factor, 
$$HF_n = \frac{E_n}{E_1}$$

Total harmonic distortion is a measures of how different is the actual waveform from its fundamental component

Total Harmonic Distortion, 
$$THD = \frac{1}{E_1} \left( \sum_{n=3,5,..}^{\infty} E_n^2 \right)^{\frac{1}{2}} = \frac{E_h}{E_1}$$

Harmonic factor is a measures of effectiveness in reducing unwanted harmonics using filters

Distortion Factor, 
$$DF = \frac{1}{E_1} \left( \sum_{n=3,5,..}^{\infty} \left( \frac{E_n}{n^2} \right)^2 \right)^{\frac{1}{2}}$$

#### Comparison of parameters in Half Bridge and Full Bridge Inverters

	Full Bridge	Half Bridge
Output voltage	$E_O = E_{DC}$	$E_O = \frac{E_{DC}}{2}$
Fundamental output voltage	$E_1 = \frac{2\sqrt{2}}{\pi} E_{DC} = 0.9 E_{DC}$	$E_1 = \frac{2\sqrt{2}}{\pi} \frac{E_{DC}}{2} = 0.45 \ E_{DC}$
Harmonic output voltage	$E_{h} = 0.4352 E_{DC}$	$E_{h} = 0.2176 E_{DC}$
Peak breaking voltage of switches	$E_{BR} = E_{DC}$	$E_{BR} = E_{DC}$

## Example

A single phase full bridge inverter is operated from 48 V battery and supplying power to a 24 ohm load. Determine output power THD of output and transistor ratings.

#### Solution:

RMS Power, 
$$P = \frac{E^2}{R} = \frac{48^2}{24} = 96 \text{ W}$$

$$E_1 = 0.9 E_{DC} = 0.9 \times 48 = 43.2 \text{ V}$$

$$E_h = 0.4352 E_{DC} = 0.4352 \times 48 = 20.89 \text{ V}$$

$$THD = \frac{E_h}{E_1} = \frac{20.89}{43.2} = 48.36\%$$

$$V_{CE} \geq 48 \; \mathrm{V}$$

$$\frac{E_{DC}}{R} = \frac{\frac{E_{DC}}{R}}{\frac{48}{24}} = 2A$$

# **Cross Conduction or Shoot Through Fault**



- Normally the switches in the bridge switch on in pairs – S1-S2 turn on first and after they are off, S3-S4 turn on
- Therefore the switches in the same leg (say S1 and S4) may not turn on at the same time
- Due to turn off delay, incoming device and outgoing device of the same leg in the bridge conduct at the same instant and short circuits the DC source.
- This fault damages both the devices

# **Cross Conduction or Shoot Through Fault**



- A solution for cross conduction fault is to introduce a dead band or delay between the trailing edge of the gate input of outgoing device and the leading edge of the gate input of incoming device
- Dead band should be longer than the turn off time of the inverter



## **3-Phase Inverter**



Load configurations











Interval	Incoming Device	Conducting Devices
1	S1	5,6,1
2	S1	6,1,2
3	S3	1,2,3
4	S4	2,3,4
5	S5	3,4,5
6	S6	4,5,6



# Features of 180 degree conduction

- $\hfill\square$  Conduction period for each switch is 180°
- Three switches conduct at a time
- There is possibility of cross conduction if a dead band delay is not deliberately introduced.
- Phase voltages are six step waves
- Line voltages are quasi square waves





Connection during first interval







Connection during second interval







Connection during third interval







Interval	Incoming Device	Conducting Devices
1	S1	6,1
2	S1	1,2
3	S3	2,3
4	S4	3,4
5	S5	4,5
6	S6	5,6



# Features of 120 degree conduction

- $\Box$  Conduction period for each switch is only 120°
- Only two switches conduct at a time
- Two switches in the same leg of bridge have inherent dead band of 60° and there is no possibility of cross conduction
- Phase voltages are quasi square waves
- Line voltages are six step waves



## Parallel Inverter



- SCRs can be used as switch, simple forced commutation is possible
- When T1 is turned on, the transformer is energised in one direction and the capacitor C is charged with a voltage of 2E<sub>DC</sub>
  - When T2 is turned on capacitor voltage is applied to T1 in reverse direction and commutates it; the capacitor C is charged with a voltage of -2E<sub>DC</sub>
- T1 is turned on again forcing T2 to turn off and the cycle repeats
- Higher output voltage is possible by suitable transformer turns ratio

# Voltage Control with Pulse Width Modulation

#### Single Pulse width Modulation

- Consists of a pulse with variable width in each half cycle
- width varies from 0 to π

#### Multiple Pulse Width Modulation

 Is an extension of single PWM and uses several equidistant pulses in each half cycle



#### Sinusoidal Pulse Width Modulation

 Pulse width is a sinusoidal function of angular position of the pulse in a cycle



## Single Pulse PWM







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RMS value of output voltage, 
$$V = V_{DC} \left[ \frac{2d}{\pi} \right]^{\frac{1}{2}}$$

Peak value of nth harmonic, 
$$V_{onm} = \frac{4 V_{DC}}{n \pi} \sin nd$$

When pulsewidth is  $120^\circ$ , d =  $60^\circ$ 

Then peak value of 3rd harmonic,  $V_{o3m} = \frac{4 V_{DC}}{3\pi} \sin 3 \times 60 = 0$ 

This implies, when the pulse width is 120°, third harmonics will be eliminated

## Multiple Pulse PWM



# Sine PWM



Modulation Index,  $MI = \frac{V_r}{V_c}$ 

where  $V_r$  is the peak of reference wave and  $V_c$  is the peak of carrier wave

There will be low order harmonics when *MI* is greater than 1

# **Typical MOSFETS**









